

**SQUARES OF SQUARE DIFFERENCE LABELING ON PATH RELATED GRAPH**

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**Abstract**

Let  $G(V, E)$  be a graph with  $p$  vertices and  $q$  edges. Let  $f: V(G) \rightarrow \{0, 1, 2, \dots, p-1\}$  be a bijection. Define  $f^*: E(G) \rightarrow N$  by  $f_{ssd}^*(uv) = \left[ (f(u))^2 - (f(v))^2 \right]^2, \forall uv \in E(G)$ . If  $f_{ssd}^*$  is injective then  $f_{ssd}^*$  is called squares of square difference labeling of  $G$ . A graph  $G$  which admits squares of square difference labeling is called squares of square difference graph. We applied squares of square difference labeling to Path related graphs

**1. Introduction**

Every graph in this paper are simple finite, undirected and non-trivial graph  $G = (V, E)$  with vertex set  $V$  and Edge set  $E$ . For graph theoretic terminology we refer to Harary. The square sum labeling is defined by V. Ajitha, S. Arumugam and K. A. Germina.

We have improved to the square of square difference and we investigated it for path related graph

**2. Definition****Definition 2.1**

A Path  $P_n$  in a graph is a sequence of edges, each one incident to the next.

**Definition 2.2**

A Path  $P_n^2$  is a graph is obtained by appending  $v_i v_{i+1}$  and  $v_j$  and  $v_{j+2}$  for  $1 \leq i \leq n-1$  and  $1 \leq j \leq n-2$

**3. Theorems**

**Theorem 3.1** The Path graph  $P_n$  is a squares of square difference graph.

**Proof**

Let  $V = \{v_i / 1 \leq i \leq n\}$  be the vertex set of  $P_n$  graph.

Let  $E = \{v_i v_{i+1} / 1 \leq i \leq n-1\}$  be the edge set of  $P_n$  graph.

Here  $|V(G)| = n$  and  $|E(G)| = n-1$ .

Define  $f: V \rightarrow \{0, 1, 2, \dots, p-1\}$  by

$$f(v_i) = i - 1; 1 \leq i \leq n$$

Clearly  $f$  is a bijection.

Then the corresponding edge label are as follows

$$\begin{aligned} f_{ssd}^*(v_i v_{i+1}) &= [[f(v_i)]^2 - [f(v_{i+1})]^2]^2 = [i^2 - 2i + 1 - i^2]^2 \\ &= [-2i + 1]^2 = 4i^2 + 1 - 4i; \forall 1 \leq i \leq n - 1. \end{aligned}$$

Clearly the edge labels are distinct.

$P_n$  is a square of square difference graph.

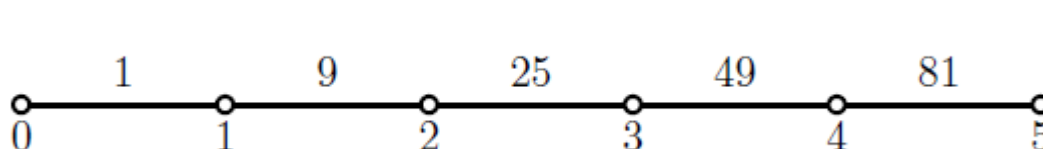


Figure 3.1

**Theorem 3.2** The Path graph  $P_n^2$  is a squares of square difference graph.

**Proof**

Let  $V = \{v_i / 1 \leq i \leq n\}$  be the vertex set of  $P_n^2$  graph.

Let  $E = \{v_i v_{i+1} / 1 \leq i \leq n - 1\} \cup \{v_i v_{i+2} / 1 \leq i \leq n - 2\}$  be the edge set of  $P_n^2$  graph.

Here  $|V(G)| = n$  and  $|E(G)| = 2n - 3$ .

Define  $f: V \rightarrow \{0, 1, 2, \dots, p - 1\}$  by

$$f(v_i) = i - 1; 1 \leq i \leq n$$

Clearly  $f$  is a bijection.

Then the corresponding edge label are as follows

$$\begin{aligned} f_{ssd}^*(v_i v_{i+1}) &= [[f(v_i)]^2 - [f(v_{i+1})]^2]^2 = [i^2 - 2i + 1 - i^2]^2 \\ &= [-2i + 1]^2 = 4i^2 + 1 - 4i; \forall 1 \leq i \leq n - 1. \end{aligned}$$

$$\begin{aligned} f_{ssd}^*(v_i v_{i+2}) &= [[f(v_i)]^2 - [f(v_{i+2})]^2]^2 = [i^2 - 2i + 1 - (i^2 + 2i + 1)]^2 \\ &= [-4i]^2 = 16i^2; \forall 1 \leq i \leq n - 1. \end{aligned}$$

Clearly the edge labels are distinct.

$P_n^2$  is a square of square difference graph.

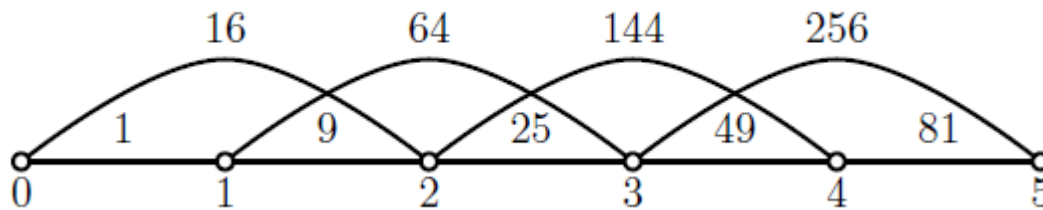


Figure 3.2

#### 4 Conclusions

In this paper, we proved Path  $P_n$  graphs and  $P_n^2$  graphs are squares of square difference graphs. There may be interesting squares of square difference graphs can be constructed in future.

#### References

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